Crystal Chemistry and Structure of Na₂SO₄(I) and Its Solid Solutions*

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Abstract

In the high-temperature polymorph Na₂SO₄(I) up to 30% cation vacancies can be generated by substitution of Na⁺ by bi- and trivalent ions. Phase diagrams and lattice parameters of these solid solutions are presented. The hexagonal high-temperature form and its monoclinic distortions can be quenched to room temperature. A structure determination was carried out. Structural and experimental data are: $P6_3/mmc$, a = 5.326 (2), c = 7.126 (3) Å, V = 175.06 Å³, Z = 2, $D_x = 2.695$ Mg m⁻³, λ (Ag $K\alpha$) = 0.55936 Å, R = 0.09for 165 reflections. The crystal structure is characterized by strong orientational disorder of the SO₄ tetrahedra. The disorder, aliovalent solid solutions, thermal expansion and ionic conductivity are discussed.

Introduction

 Na_2SO_4 has four well established modifications and a rather complicated transition behavior, which is discussed elsewhere (Mehrotra, Hahn, Eysel & Arnold, 1984). The following phase transitions occur:

$$(V) \xleftarrow{^{473}K} (III) \xleftarrow{^{503}K} (II) \xleftarrow{^{510}K} (I) \xleftarrow{^{1156}K} Liquid.$$

In the present paper only the hexagonal hightemperature form, $Na_2SO_4(I)$, is of interest. It transforms spontaneously and reversibly into the structurally related polymorph $Na_2SO_4(II)$. As a consequence, pure $Na_2SO_4(I)$ cannot be quenched to room temperature. Stabilization, however, is possible with various solid solutions.

Na₂SO₄(I) is particularly flexible in forming solid solutions: Na⁺ (r = 1.0 Å) can be completely replaced by the much larger K⁺ (1.3 Å) (Eysel, 1973) and to a large extent by aliovalent ions M^{2+} and M^{3+} . In addition, unlimited substitution of the SO₄ tetrahedra

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by the much smaller planar CO₃ triangles is known (Mehrotra, 1973). Also, combined substitutions, M^{3+} for Na⁺ and CO₃²⁻ for SO₄²⁻, have been synthesized (Schubert & Eysel, 1980). In this paper the substitution of Na⁺ by bi and

In this paper the substitution of Na⁺ by bi- and trivalent ions, resulting in high cation-vacancy concentrations, is reported. The pronounced ionic conductivity based on these vacancies has been described by Höfer, Eysel & von Alpen (1981).

The structure type of $Na_2SO_4(I)$ is the hightemperature structure of many $A_2[BX_4]$ compounds. Several structure proposals and determinations have been described but an unambiguous result is still missing. This is mainly due to a lack of suitable single crystals and the occurrence of disorder phenomena. As a contribution to this problem a structure determination, using a stabilized single crystal of $Na_2SO_4(I)$, is reported.

Experimental

Powder samples were prepared from analytical-grade sulfates (Merck, Koch-Light) which were melted for a few minutes in Pt crucibles and quenched in air. Investigations were performed with a Norelco powder diffractometer and a high-temperature Guinier camera. For the determination of the phase diagrams annealing experiments at various subsolidus temperatures were carried out. The single crystals for the structure determination were obtained by slowly cooling a sample of composition $(Na_{0.94}Y_{0.02}\square_{0.04})_2SO_4$ (\square = vacancy) from the melt down to 600 K and subsequently quenching. The crystals contained $1\cdot 2 \mod^{9} Y_2(SO_4)_3$ which is the minimal amount that stabilizes form (I). Crystal dimensions $0 \cdot 136 \times 0 \cdot 153 \times$ $0 \cdot 340 \text{ mm}.$

Data collection: automatic single-crystal diffractometer (AED, Siemens); Ag $K\alpha$ radiation ($\lambda = 0.55936$ Å); lattice parameters refined from powder diffractometer data; 1200 reflections up to $2\theta = 53^{\circ}$, with $-2 \le h \le 8, -2 \le k \le 9, -2 \le l \le 11$; 216 independent reflections, 165 with $|F_o| > 2\sigma(F_o)$; F(000) =140; Lorentz and polarization corrections, no absorption or extinction corrections. Measurements of the

^{*} Presented at the Tenth and Eleventh International Congresses of the International Union of Crystallography held in Amsterdam (Keester, Eysel & Hahn, 1975) and Warsaw (Höfer, von Alpen & Eysel, 1978), respectively.

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standard reflection $\overline{222}$ at regular intervals showed deviations with time of less than 2% in intensity. There was an unusual decrease of intensities with $\sin \theta/\lambda$. Fourier and full-matrix least-squares refinements [using F_o and weights $1/\sigma(F_o)$] were performed with the XRAY system of crystallographic programs (Stewart, Kruger, Ammon, Dickinson & Hall, 1972).* Atomic scattering factors for neutral atoms Na, S and O were taken from International Tables for X-ray Crystallography (1974). The results were reproduced with a second crystal measured on another single-crystal diffractometer (CAD-4, Nonius).

Solid solutions of $Na_2SO_4(I)$

The phase diagrams of many Na₂SO₄- M^{2+} SO₄ ($M^{2+} = Mg$, Ni, Zn, Cd, Ca, Pb, Ba, etc.) systems have been described, and extended solid-solution series for Na₂SO₄(I) have been reported (Table 1). For several systems the results were confirmed by reinvestigation. As an example, the phase diagram of the system Na₂SO₄-NiSO₄ is shown in Fig. 1. Surprisingly, Na₂SO₄(I) also forms solid solutions in Na₂SO₄- $M_2^{3+}(SO_4)_3$ systems (Table 1). Fig. 2 shows the Na₂SO₄-rich part of the system Na₂SO₄- $Y_2^{3+}(SO_4)_3$.

Even though these aliovalent substitutions have been known since about 1910 (see references in Table 1), the structural background has never been discussed. Crystal-chemical reasons suggest the substitution types $2Na^{2+} = 1M^{2+} + 1\Box$ and $3Na^{+} = 1M^{3+} + 2\Box$, corresponding to the formulae $Na_{2-2x}M_x^{2+}\Box_xSO_4$ and $Na_{2-2x}M_{2x/3}^{3+}\Box_{4x/3}SO_4$, which

* A list of structure factors has been deposited with the British Library Lending Division as Supplementary Publication No. SUP 39504 (6 pp.). Copies may be obtained through The Executive Secretary, International Union of Crystallography, 5 Abbey Square, Chester CH1 2HU, England.

1273 K Liquid 1156 1073 963 K -NISO 923 K 873 lss ά 748 K 673 698 K ₂(SO₄)₂ NiSO4 510 NiNa₆(SO, NiNa₂ 473 ά 423 K ш 273 20 40 60 80 100 0 mol% NiSO₄ Na₂SO₄

Fig. 1. Phase diagram of the system Na₂SO₄-NiSO₄. The very small area of Na₂SO₄(II) (s.s.) has been omitted.

Table 1. Na₂SO₄(I) solid solutions with M^{2+} SO₄ and M_2^{3+} (SO₄)₃

Limit of solid		
solution mol% $M^{2+}SO_4$ or $M_2^{3+}(SO_4)_3$	% cation vacancies	Reference [†]
25	12.5	(1), (2)
36	18	(3)
30	15	(4), (5)
35	17.5	(1)
30	15	(6)
55	27.5	(7)
40	20	(8)
40	20	(2), (9), (10)
17	8.5	(2)
17	8.5	(11), (12)
21	10-5	(13)
>2.5		(2)
14	22	(5)
>2.5*		(2)
20	29	(2)
>2.5*		(2)
>2.5*		(2)
>2.5*		(2)
	Limit of solid solution mol% $M^{2+}SO_4$ or $M^{2+}SO_{4})_3$ 25 36 30 35 30 55 40 40 40 17 17 21 >2.5 14 >2.5 14 >2.5 14 >2.5* 20 >2.5* 20 >2.5* >2.5* >2.5*	Limit of solid solution mol% $M^{2+}SO_4$ % cation or $M_2^{3+}(SO_4)_3$ % cation vacancies 25 12.5 36 18 30 15 35 17.5 30 15 55 27.5 40 20 40 20 17 8.5 21 10.5 >2.5 14 22 >2.5* 20 29 >2.5* >2.5* >2.5*

* Form (1) was stabilized with 2.5 mol% of sulfates $M_2^{3+}(SO_4)_3$. The limits of solid solution are probably much higher.

† (1) Bol'shakov & Fedorov (1956). (2) This paper. (3) Ginsberg (1909).
(4) Bellanca & Carapezza (1951). (5) Bol'shakov, Fedorov & Ilina (1963).
(6) Evseeva (1953). (7) Calcagni & Marotta (1915). (8) Calcagni & Marotta (1913). (9) Müller (1910). (10) Bellanca (1942). (11) Calcagni & Marotta (1912).
(12) Perrier & Bellanca (1940). (13) Calcagni (1912).

were confirmed indirectly by the results of ionicconductivity measurements (Höfer, Eysel & von Alpen, 1981). Up to about 30% cation vacancies can be generated in the $Na_2SO_4(I)$ structure.

With increasing amounts of M^{2+} and M^{3+} ions the X-ray powder diffraction peaks become broader, indicating decreasing perfection. On cooling *pure* Na₂SO₄, the transition sequence Na₂SO₄(I) \rightarrow Na₂SO₄(II) \rightarrow Na₂SO₄(II) \rightarrow Na₂SO₄(II) \rightarrow Na₂SO₄(II) \rightarrow Na₂SO₄(II) is observed, with form (III) occurring at room temperature. In solid solutions, however, it is possible to quench the high-temperature form (I). The lattice parameters of quenched samples in Figs. 3 and 4 exhibit opposite slopes of *a* and *c*, with nearly constant cell volumes. The lattice parameters of pure Na₂SO₄(I) at room temperature can be extrapolated to a = 5.36 Å and



Fig. 2. Part of the phase diagram of the system $Na_2SO_4-Y_2(SO_4)_3$.

Table 2. Lattice parameters of quenched Na₂SO₄(I) solid solutions at 293 K (except for pure Na₂SO₄)

(Pseudo-)orthohexagonal axes. Standard deviations ± 0.01 Å for the first two and ± 0.003 Å for the subsequent materials.

Composition	Symmetry	a(Å)	b(Å)	c(Å)	Angle (°)	$V(Å^3)$	a/b
Na2SO4(I), 543 K	$P6_3/mmc$	9.39	5.42	7.24		368.5	$\sqrt{3} = 1.7321$
$Na_2SO_4(1)$, 293 K*		9.28	5.36	7.06		351-2	√3
Na1-88Y0-04 0-08SO4		9.225	5.326	7.126		350-1	√3
$Na_{1.61}Y_{0.13}\Box_{0.26}SO_4$		9.154	5.285	7.262		351-3	√3
Na1-80 Ni0-10 0-10 SO4		9.209	5.317	7-114		348.3	√3
$Na_{1.80}Sr_{0.10}\square_{0.10}SO_4$		9.273	5-354	7.175		356-2	√3
$Na_{1.60}Zn_{0.20}\Box_{0.20}SO_4$		9.246	5.338	7.119		351-4	√3
$Na_{1.90}Zn_{0.05}\square_{0.05}SO_4$	Monoclinic	9.265	5.348	7.121	$\beta = 92 \cdot 37$	352.5	1.7324
$Na_{1.60}Ca_{0.20}\Box_{0.20}SO_4$		9.246	5.338	7.134	$\alpha = 91 \cdot 37$	352-1	1.7321

* Extrapolated from Figs. 3 and 4.

c = 7.06 Å (Table 2). The scales of the cation vacancies and of the lattice parameters in Figs. 3 and 4 are the same for both series. The very similar slopes of the curves show that the lattice parameters are controlled predominantly by the vacancy concentration and less by the sizes and valencies of the substituting ions. The same dependence was found for the ionic conductivity.

If the samples are cooled slowly, two different monoclinic distortions may be observed (Table 2). The type with $\beta \neq 90^{\circ}$ was found for solid solutions with Zn^{2+} , Ca^{2+} and Y^{3+} . The second type with $\alpha \neq$ 90° was obtained only with high Ca^{2+} contents (>9 mol% CaSO₄). On heating in a high-temperature Guinier camera the latter type transformed to the former just before becoming hexagonal. Powder data of the hexagonal and the two monoclinic varieties are published in the JCPDS Powder Data File (Card Nos. 29-1290, 29-1196, 29-1291).

Disorder models

In this study for the first time $Na_2SO_4(I)$ single crystals suitable for structure determination were available. This structure type, despite the simple chemical formula, is by no means trivial, and its rather compli-



Fig. 3. Lattice parameters and cell volume of $Na_2SO_4(I)$ solid solutions in the system Na_2SO_4 -NiSO₄. \Box = cation vacancy.

cated disorder has led to conflicting results in the literature.

The following structural features are common to all experimental results on $Na_2SO_4(I)$ and isostructural compounds.

(i) Small hexagonal cell (Table 2), containing only four cations and two tetrahedra.

(ii) Simple 'basic structure' of Fig. 5; the large spheres symbolize the SO_4 tetrahedra without regard to their orientation.

(iii) Laue class 6/mmm and a tertiary c glide, resulting in the possible space groups $P6_3/mmc$, $P6_3mc$, and $P\overline{6}2c$. These results were confirmed in the present study.

(iv) Existence of secondary (vertical) mirror planes in the structure, thus excluding $P\overline{6}2c$.

Discrepancies among authors, however, exist with respect to the orientation of the tetrahedra. For the subsequent discussion a tetrahedron is represented by an arrow, as shown in Fig. 6(a). The direction of the arrow indicates the orientation of that tetrahedral apex which points along or nearly along the threefold



Fig. 4. Lattice parameters and cell volume of $Na_2SO_4(I)$ solid solutions in the system $Na_2SO_4-Y_2(SO_4)_3$.

axis. Based on the ordered structure, symbolized by Fig. 6(b) (polar space group $P6_3mc$), several types of orientational disorder of the tetrahedra have to be considered:

(1) 'up-down' disorder,* resulting in a mirror plane perpendicular to the c axis (centrosymmetric space group $P6_3/mmc$, Fig. 6c);

(2) 'tilting' disorder due to inclination of the 'split' tetrahedra against the trigonal axis with α = tilting angle ($P6_3mc$, Fig. 6d);

(3) 'left-right' disorder with respect to the vertical mirror plane ($P6_3mc$ and $P6_3/mmc$, not illustrated);

(4) combination of (1) and (2) $(P6_3/mmc, Fig. 6e)$;

(5) the tilting angle $\alpha = 31.5^{\circ}$ represents a special case for which (2) and (4) become identical, because all split tetrahedra have one edge parallel to the *c* axis ($P6_3/mmc$, Fig. 6*f*).

Most of these possibilities have been considered in the literature:

Fig. 5: Bredig (1943) for Na_2SO_4 and K_2SO_4 , rotation of SO_4 groups;

Fig. 6(b): Eysel & Hahn (1970) for α -Ca₂SiO₄; Iwai, Sakai & Watanabe (1973) for high-K₂SO₄; Mehrotra (1973) for high-Na₂SeO₄; Kobayashi & Saito (1982) for Na₂SO₄(1);

Fig. 6(c): Fischmeister (1962), van den Berg & Tuinstra (1978), Miyake, Morikawa & Iwai (1980), all for high-K₂SO₄;

Fig. 6(d): De Wolff (1970, private communication) for high-K₂SO₄;

Fig. 6(f): Höfer (1979) and the present paper for Na₂SO₄(I); Arnold, Kurtz, Richter-Zinnius, Bethke & Heger (1981) for high-K₂SO₄.

In the sequel the average structure of $Na_2SO_4(I)$ is described and an attempt is made to interpret it on the basis of the disorder models above.

* Ordered up-down arrangements occur in several related crystal structures, e.g. $NaK_3(SO_4)_2$ (glaserite) and low- K_2SO_4 .



Fig. 5. 'Basic structure' for Na₂SO₄(1). Small spheres Na, large spheres SO₄ tetrahedra. Space group P6₃/mmc.

Structure determination

Statistical methods, such as the N(z) test, allowed no distinction between space groups $P6_3mc$ and $P6_3/mmc$, nor did investigations with a secondharmonic analyzer.

Fourier computations were carried out based upon the polar models in Figs. 6(b) and 6(d) and the centrosymmetric models in Figs. 6(c), 6(e), and 6(f). For the noncentrosymmetric models all phases were close to 0 or π . Moreover, it turned out that for *all* models corresponding structure factors received very nearly the same phases. As a consequence, the calculated electron density is model-invariant within the accuracy of the method.

The Fourier sections $\rho(xy\frac{1}{4})$, $\rho(xy\frac{1}{15})$, and $\rho(\bar{x}xz)$ are shown in Figs. 7 and 8. The most remarkable result is the fact that the centers of the S and of three O maxima are located on the same level $z = \frac{1}{4}$, simulating a planar SO₃ group. In $\rho(xy_{\frac{1}{4}})$ the S maxima are circular whereas the O contours show a slight elongation normal to the S-O direction. In $\rho(xy_{15}^{\perp})$, *i.e.* 1.3 Å from $z = \frac{1}{4}$, the S atom has vanished but the O atoms are still visible. This is also evident from $\rho(\bar{x}xz)$ which, in addition, shows a peculiar banana-shaped distribution of the O density. The S atom is slightly elongated along the c axis (non-equidistant contours in Fig. 8 simulate a stronger elongation). No electron density at all is found on the trigonal axis above and below the S atom. This excludes the disorder models in Figs. 6(b) and 6(c).

The observed electron density was interpreted by fitting regular SO₄ tetrahedra with S-O distances of 1.47 Å. The only agreement was obtained for the model of Fig. 6(f) with the special tilting angle $\alpha =$ 31.50°. For this angle the 'upper' and 'lower' member of each pair of tetrahedra in Fig. 6(e) merge and the population parameter (p.p.) is increased to $\frac{1}{3}$. The



Fig. 6. Representation of possible tetrahedral orientations in the structure of $Na_2SO_4(1)$ by arrows; p polar, np non-polar, o ordered, u up-down disorder, t tilting disorder, pp population parameter.

resulting arrangement is shown in Fig. 9. It consists of three superimposed split tetrahedra, each with one edge parallel and one perpendicular to the c axis. In Figs. 7 and 8 the O and S positions of the model are marked by crosses; the three split tetrahedra are designated A, B, and C. The close agreement between the Fourier maxima and the crosses proves the correctness of the proposed structure, as do the rather flat features in the final difference Fourier synthesis.

Numerous full-matrix least-squares refinements were carried out, varying the positional parameters defined by the different models, as well as isotropic temperature factors of all atoms. This resulted in a weighted R factor $R_w = 0.093$ which is higher than usual owing to the strong disorder. The continuous electron density of the O atoms, however, precludes a meaningful refinement of individual atomic positions and bond lengths. Indeed, the least-squares calculations did not lead to a significant and chemically reasonable improvement of the structure; instead, high temperature factors resulted. For this



Fig. 7. Electron density sections of Na₂SO₄(1). (a) $\rho(xy_4^{\perp})$, (b) $\rho(xy_{15}^{\perp})$. The three equivalent tetrahedra are designated A, B, and C. An asymmetric unit is outlined. Crosses are atomic positions of the model in Fig. 6(f).

reason, in Table 3 the positional parameters derived from the model (without standard deviations) are listed; the isotropic temperature factors B were obtained from the least-squares calculations.

The above interpretation of the observed electron density is supported by the following facts.



Fig. 8. Electron density section $\rho(\bar{x}xz)$ of Na₂SO₄(I). The three equivalent tetrahedra are designated A, B and C. Note that the contours of the S peak are not equidistant. Crosses are atomic positions of the model in Fig. 6(f).



Fig. 9. Interpretation of the average structure of $Na_2SO_4(I)$ in terms of the orientational disorder of the tetrahedra. Some representative Na-O bonds are indicated by dashed lines. The remaining bonds are obtained by applying the symmetry operations of space group $P6_3/mmc$. The O atoms are labeled as in Table 3.

Table 3. Positional parameters (see text) and isotropic temperature factors in $Na_2SO_4(1)$

Ideal SO₄ tetrahedra with d(S-O) = 1.47 Å are assumed.

	Multiplicity, Wyckoff letter	x	у	z	$B(\text{\AA}^2)$
Na	2 d	13	2	3 4	6.2(2)
Nan	2 a	ō	Ő	õ	3.3(1)
S	2 c	13	2 3	1	4.5 (2)
OI	12 k	0.242	0.484	0.418	9.1 (3)
Ou	12 j	0.199	0.346	1	4.8(2)

(a) It is the only model which explains the coplanar arrangement of the S and O_{11} maxima in Figs. 7(a) and 8.

(b) The rather sharp S maximum proves that the centers of the three split tetrahedra very nearly coincide.

(c) The three (elongated) O maxima in $\rho(xy_4^1)$ represent six O atoms, two from each of the three split tetrahedra A, B, and C (cf. upper part of Fig. 9).

(d) The remaining six O atoms of the model are located above and below the mirror plane, at about $z = \frac{1}{15}$ and $\frac{7}{15}$. They form the upper and lower part of the 'banana' in Fig. 8 and are visible as small peaks in Fig. 7(b) (cf. lower part of Fig. 9). The low electron density at the positions of these atoms, however, is unsatisfactory and a weakness of the model.

(e) No significant indication for disorder of the Na atoms was observed.

Because of the disorder no individual Na coordination polyhedra can be defined. The average coordinations of the two Na atoms (obtained by reducing the Na-O bonds to unit weight), are quite different: Na₁ has four close (2.52 Å), two intermediate (2.80 Å), and four rather distant (3.00 Å) O neighbors. In contrast, Na₁₁ is surrounded by six close and rather equidistant O atoms (2.31-2.40 Å).

Discussion

From the previous section it is evident that the feature characterizing the $Na_2SO_4(I)$ structure is a strong positional disorder of the SO₄ tetrahedra. Whereas the Na and S atoms are rather well resolved, for the O atoms this is true only in the horizontal xy plane; in the vertical $\bar{x}xz$ plane, however, the O atoms are not resolved at all. The methods employed so far do not allow a distinction between dynamic or static (frozen-in high-temperature equilibria) disorder; 'normal' anisotropic thermal motion, however, can be excluded, both because of the unusually large disorder effect and because the measurements were made at room temperature on quenched metastable crystals. (Unfortunately, the search for domains with an electron microscope failed owing to vaporization of the sample.) The split model in Figs. 6(f) and 9 with its well defined atomic positions, therefore, must be considered as a limiting case upon which further 'continuous' (positional or thermal) disorder of the tetrahedra around the S atoms is superimposed. At higher temperatures certainly the thermal component will gain in importance.

Even though the crystals investigated are metastable at room temperature and contain small amounts of Y atoms, as well as cation vacancies, the authors believe that the proposed structure represents the average high-temperature state in the stability range of form (I) (above 510 K). Comparison with high-temperature powder and single-crystal patterns of pure Na₂SO₄(I) revealed no differences.

The increase in thermal motion with temperature will result in an elongation of the banana which may lead to a participation of the 'up-down disorder' in Fig. 6(c). This strong c component of the thermal motion is reflected in the extraordinary anisotropy of the thermal expansion of Na₂SO₄(1) which in the c direction is two to three orders of magnitude larger than in the a direction.

The tetrahedral disorder is also probably the reason for the unusual unlimited SO_4 - CO_3 substitution in $Na_2SO_4(I)$. Moreover, the variety of local cation coordinations favors the aliovalent cation substitution. For the structurally related ordered polymorphs $Na_2SO_4(II)$ and $Na_2SO_4(III)$ no comparable solid solutions were found.

It should be noted that the tetrahedral disorder is not the only reason for the unusual ionic conductivity, since $Na_2SO_4(I)$ becomes a fast ionic conductor only if extrinsic cation vacancies are introduced by aliovalent substitution. Owing to oscillation of the tetrahedra the Na^+ ions can easily move from vacancy to vacancy. Thus, dynamic disorder seems more compatible with the ionic conductivity than static disorder.

It is gratifying that a similar disorder type was found for high-K₂SO₄ at 847 and 913 K by Arnold, Kurtz, Richter-Zinnius, Bethke & Heger (1981), using single-crystal neutron diffraction, and at 1073 K, by Miyake, Morikawa & Iwai (1980) with single-crystal X-ray diffraction. Density maps comparable to those in this study were found and interpreted by Arnold et al. in favor of the 'edge' model (Fig. 6f) with a small contribution of the 'apex' model (Fig. 6c), whereas Miyake et al. found only the apex model at 1073 K. Thus the three studies, even through differing in detail, strongly support each other and show that the tetrahedral disorder is not a feature of the particular compounds but rather of the whole structure type. With increasing temperature the 'up-down disorder' (Fig. 6c) probably strongly gains in importance.

The high-temperature forms of a large number of $M_2[TX_4]$ compounds are considered to be isostructural with Na₂SO₄(I). The assignment is usually based on high-temperature powder diagrams. It must be noted, however, that different kinds of disorder which are based on subgroups of $P6_3/mmc$ result in very similar powder patterns. This applies in particular to the disorder types in Fig. 6.

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Investigation of Superlattices in K_xWO₃ in Relation to Electric Transport Properties

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Abstract

Single crystals of $K_x WO_3$ were investigated with electron microscopy and X-ray diffraction methods. In most cases deviations from the hexagonal tungsten bronze structure in terms of commensurate and apparently incommensurate superlattices were observed. The commensurate superlattices in the *a*-*b* plane of the hexagonal lattice were, for most compounds, relatively simple, resulting in either an

orthohexagonal unit cell or a hexagonal unit cell with two or four times the volume of the tungsten bronze structure, respectively. The 'incommensurate' superlattice rows in the c direction indicated a periodicity of 50 to 250 Å or more, depending in part on the crystal composition and temperature. Several different superlattice phases were observed. The superlattice formation is believed to be caused by ordering of the potassium atoms within the channels of the tungsten bronze structure. The data are consistent

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